



# Productivity and Efficiency Analysis

## Basic Commands in STATA

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## Recapping... (Textbook: Coelli - Rao - O'Donnell - Battese)

### \* For Decision-Making Units (DMUs):

**Productivity:** Output / Input

**Efficiency:** Productivity / (Benchmark Productivity), where

Output: **variables** (measures of Y, e.g. #items, TR)

Input: **variables** (measures of X, e.g. K, L, E, N, H)

### \* Methods of Analysis:

for **Productivity:** Total Factor Productivity, Partial Indicators

for **Efficiency:** Non-Parametric (NP) & Parametric (P) ways

NP: **DEA**, FDH

P: COLS, **SFA** (FE, GLS, RE)

## DEA (Data Envelopment Analysis) in Stata

### \* Get do-file "dea"

which dea : confirming local (in)existence of package  
findit dea : looking for the .ado file in Stata websites  
net install st0193 : installing (Or put **dea.ado** in c:/ado)

### \* Prepare your dataset - keep variables in columns

use (filename OR w.d. filename) : choosing dataset  
generate dm\_u = \_n : numbering our DMUs

### \* Apply the dea syntax

dea ivars = ovars, rts(crs|vrs|drs|nirs) ort(in|out)  
stage(1|2) trace saving(results-filename)

## DEA (Data Envelopment Analysis) in Stata - continued

### \* Choose your arguments

ivars = input variable list, e.g. workHours rndExpenses

ovars = output variable list, e.g. totalRevenues numberItems

rts = returns to scale (**const.**, var., decr., non incr.)

ort = orientation (**input**, output)

stage = number of stages (1, 2)

trace = saving intermediate results in the **dea.log** file

saving = specifying a (filename).**dta** file for storing final results

### \* Results in memory

r(dearslt) =  $n \times m$  matrix, where  $n$  is the number of DMUs and  $m$  includes all used inputs, outputs, slacks, ranks (DMU scores), theta (efficiency scores), reference DMUs etc

## DEA: Example

```
. use "C:\res-dea.dta", clear
. dea weight Volume = fuel_consumption, rts(crs) ort(out)
```

```
options: RTS(CRS) ORT(OUT) STAGE(2)
CRS-OUTPUT Oriented DEA Efficiency Results:
```

|       | rank | theta   | ref: | ref: | ref:    |
|-------|------|---------|------|------|---------|
|       |      |         | 1    | 2    | 3       |
| dmu:1 | 4    | 1.50865 | 0    | 0    | 7.845   |
| dmu:2 | 5    | 2.91765 | 0    | 0    | 1.13524 |
| dmu:3 | 1    | 1       | 0    | 0    | 1       |
| dmu:4 | 1    | 1       | 0    | 0    | 0       |
| dmu:5 | 3    | 1.16987 | 0    | 0    | 1.23709 |

  

|       | ref:    | ref: | islack: | islack: | oslack:          |
|-------|---------|------|---------|---------|------------------|
|       | 4       | 5    | weight  | Volume  | fuel_consumption |
| dmu:1 | 0       | 0    | 0       | 20.1971 | 0                |
| dmu:2 | 5.5632  | 0    | 0       | 0       | 0                |
| dmu:3 | 0       | 0    | 0       | 0       | 0                |
| dmu:4 | 1       | 0    | 0       | 0       | 0                |
| dmu:5 | .733069 | 0    | 0       | 0       | 0                |

theta : efficiency score -> rank=1 : highest theta (most efficient DMU)

1-theta : optimization margin <- slacks : additional individual i/o margins

reference weights : calculated for most efficient DMUs

## SFA (Stochastic Frontier Analysis) in Stata

### \* Get package "frontier" and apply the frontier syntax

which frontier : (included in the Stata base .ado folder)  
frontier depvar indepvars [weight] [, options]

### \* Choose your arguments

depvar = dependent variable, indepvars = independent variables  
option vhet(varlist) : idiosyncratic-error explanatory variables  
option uheter(varlist) : technical-inefficiency explan. variables  
option distribution(**hnormal**, exponential, tnormal) : for uheter  
option cost (if it's a frontier for cost instead of productivity), etc

### \* Alternatives

help xtreg, xtfreder

## SFA: Example

```
. frontier fuel_consumption weight Volume, distribution(hnormal)
Stoc. frontier normal/half-normal model      Number of obs   =           5
                                                Wald chi2(2)    =    2.75e+08
Log likelihood = -13.937211                    Prob > chi2     =    0.0000
```

| fuel_consumption | Coef.     | Std. Err. | z     | P> z  | [95% Conf. Interval] |          |
|------------------|-----------|-----------|-------|-------|----------------------|----------|
| weight           | .2130523  | .2618734  | 0.81  | 0.416 | -.30021              | .7263147 |
| Volume           | .2169887  | .0218704  | 9.92  | 0.000 | .1741235             | .259854  |
| _cons            | 24.06524  | 1.630157  | 14.76 | 0.000 | 20.8702              | 27.26029 |
| /lnsig2v         | -26.26117 | 560.2429  | -0.05 | 0.963 | -1124.317            | 1071.795 |
| /lnsig2u         | 4.123302  | .6324557  | 6.52  | 0.000 | 2.883711             | 5.362892 |
| sigma_v          | 1.98e-06  | .0005557  |       |       | 7.2e-245             | 5.5e+232 |
| sigma_u          | 7.858933  | 2.485213  |       |       | 4.228535             | 14.6062  |
| sigma2           | 61.76283  | 39.06225  |       |       | -14.79777            | 138.3234 |
| lambda           | 3961901   | 2.485213  |       |       | 3961897              | 3961906  |

Likelihood-ratio test of sigma\_u=0: chibar2(01) = 3.63 Prob>=chibar2 = 0.028

s...- \_v, \_u, 2; l... : stdev(v), stdev(u), var(v)+var(u); stdev(u)/stdev(v)  
 H0 vs Ha (Model) : all coefficients are zero vs at least one being non-zero  
 H0 vs Ha (sigma\_u) : s...\_u =0 vs >0 (absent & present technical inefficiency)  
 Prob : if <0.05, reject the corresponding H0 with 95% confidence

## Malmquist Productivity Indicator

### \* Get do-file "malmq" - Prepare your dataset

which malmq : confirming local (in)existence of package  
 ... (find and put **malmq.ado** in c:/ado)

use (filename OR w.d. filename) : choosing dataset

generate dmU= \_n : numbering our DMUs

### \* Apply the malmq syntax (arguments like in dea)

malmq ivars = ovars, period(time-varname) ort(in|out)  
 trace saving(results-filename)

### \* For Partial Productivity...

help orderm, orderalpha



## MPI: Example

```
. malmq i_AC = O_SPI O_CPI, ort(o) period(period)
```

Cross CRS-DEA Result:

|            | from  | thru  | t       | t1          |
|------------|-------|-------|---------|-------------|
| dmu:DMU101 | 38869 | 38899 | 128.007 | 2.54674     |
| dmu:DMU115 | 38869 | 38899 | .514718 | 7.78878     |
| dmu:DMU118 | 38869 | 38899 | 64.6469 | 21.4819 ... |

Malmquist efficiency OUTPUT Oriented DEA Results:

|    | period | dmu    | CRS_eff | VRS_eff |     |
|----|--------|--------|---------|---------|-----|
| 1. | 38869  | DMU101 | 1.83388 | 1       |     |
| 2. | 38869  | DMU115 | 4.51366 | 1.12252 |     |
| 3. | 38869  | DMU118 | 12.8484 | 1.02734 | ... |

Malmquist productivity index OUTPUT Oriented DEA Results:

|    | period      | dmu    | tfpch   | effch   | techch  | pech    | sech        |
|----|-------------|--------|---------|---------|---------|---------|-------------|
| 1. | 38869~38899 | DMU101 | 72.8157 | 105.487 | .69028  | 1       | 105.487     |
| 2. | 38869~38899 | DMU115 | .121    | .22155  | .546153 | .890857 | .248693     |
| 3. | 38869~38899 | DMU118 | 4.6528  | 7.19371 | .646786 | 1.64446 | 4.37451 ... |

CRS\_eff, VRS\_eff : efficiency scores for CRS and VRS

tfpch, pech, effch, techch, sech : changes in TFP, in technical efficiency relative to VRS (pure) and CRS, technical and in scale efficiency, respectively.

## Savage Chickens

by Doug Savage



Thank you!