

$$\text{In[3]:= } \mathbf{s1 = DSolve}\left[\mathbf{y' [x] + \frac{y[x]}{x^2} == Cos[x^2], y[x], x}\right]$$

$$\text{Out[3]= } \left\{\left\{y[x] \rightarrow e^{\frac{1}{x}} C[1] + e^{\frac{1}{x}} \int_1^x e^{-\frac{1}{K[1]}} \text{Cos}[K[1]^2] dK[1]\right\}\right\}$$

$$\text{In[6]:= } \mathbf{s2 = DSolve}\left[\mathbf{y' [x] + 2 x \times y[x] == 2 x^3 \times y[x]^3, y[x], x}\right]$$

$$\text{Out[6]= } \left\{\left\{y[x] \rightarrow -\frac{\sqrt{2}}{\sqrt{1 + 2 x^2 + 2 e^{2 x^2} C[1]}}\right\}, \left\{y[x] \rightarrow \frac{\sqrt{2}}{\sqrt{1 + 2 x^2 + 2 e^{2 x^2} C[1]}}\right\}\right\}$$

$$\text{In[7]:= } \mathbf{s3 = DSolve}\left[\mathbf{y' [x] \times \sin x - y[x] \ln y[x] == 0, y[x], x}\right]$$

$$\text{Out[7]= } \left\{\left\{y[x] \rightarrow e^{\int_1^x \frac{\ln y[K[1]]}{\sin x} dK[1]} C[1]\right\}\right\}$$

$$\text{In[8]:= } \mathbf{s4 = DSolve}\left[\mathbf{y' [x] == \frac{x - y[x]}{x + y[x]}, y[x], x}\right]$$

$$\text{Out[8]= } \left\{\left\{y[x] \rightarrow -x - \sqrt{e^{2 C[1]} + 2 x^2}\right\}, \left\{y[x] \rightarrow -x + \sqrt{e^{2 C[1]} + 2 x^2}\right\}\right\}$$

$$\text{In[10]:= } \mathbf{s5 = DSolve}\left[\mathbf{x \times y' [x] + x \times y[x] == 3 \times x, y[x], x}\right]$$

$$\text{Out[10]= } \left\{\left\{y[x] \rightarrow 3 + e^{-x} C[1]\right\}\right\}$$

$$\text{In[12]:= } \mathbf{s6 = DSolve}\left[\mathbf{x \times y' [x] - 8 \times y[x] == x^3 \times \cos x, y[x], x}\right]$$

$$\text{Out[12]= } \left\{\left\{y[x] \rightarrow -\frac{\cos x x^3}{5} + x^8 C[1]\right\}\right\}$$

$$\text{In[15]:= } \mathbf{s7 = DSolve}\left[\mathbf{x \times y' [x] - \frac{y[x]}{x} == x^2 \times y[x]^5, y[x], x}\right]$$

$$\text{Out[15]= } \left\{\left\{y[x] \rightarrow -\frac{(-1)^{1/4}}{\left(-8 x + 2 x^2 - e^{4/x} C[1] - 32 e^{4/x} \text{ExpIntegralEi}\left[-\frac{4}{x}\right]\right)^{1/4}}\right\},\right. \\ \left.\left\{y[x] \rightarrow \frac{(-1)^{1/4}}{\left(-8 x + 2 x^2 - e^{4/x} C[1] - 32 e^{4/x} \text{ExpIntegralEi}\left[-\frac{4}{x}\right]\right)^{1/4}}\right\},\right. \\ \left.\left\{y[x] \rightarrow -\frac{(-1)^{3/4}}{\left(-8 x + 2 x^2 - e^{4/x} C[1] - 32 e^{4/x} \text{ExpIntegralEi}\left[-\frac{4}{x}\right]\right)^{1/4}}\right\},\right. \\ \left.\left\{y[x] \rightarrow \frac{(-1)^{3/4}}{\left(-8 x + 2 x^2 - e^{4/x} C[1] - 32 e^{4/x} \text{ExpIntegralEi}\left[-\frac{4}{x}\right]\right)^{1/4}}\right\}\right\}$$

$$\text{In[20]:= } \mathbf{s8 = DSolve}\left[\mathbf{x \times y' [x] \times y[x] - y[x]^2 + x^2 - 2 == 0, y[x], x}\right]$$

$$\text{Out[20]= } \left\{\left\{y[x] \rightarrow -\sqrt{x^2 C[1] + 2 x^2 \left(-\frac{1}{x^2} - \text{Log}[x]\right)}\right\}, \left\{y[x] \rightarrow \sqrt{x^2 C[1] + 2 x^2 \left(-\frac{1}{x^2} - \text{Log}[x]\right)}\right\}\right\}$$

$$\text{In[31]:= } \mathbf{s9 = DSolve}\left[\mathbf{x^2 \times y' [x] - (x \times y[x] - 2)^2 == 0, y[x], x}\right]$$

$$\text{Out[31]= } \text{DSolve}\left[-\left(-2 + x \frac{a}{x}[x]\right)^2 + x^2 \left(\frac{a}{x}\right)'[x] == 0, \frac{a}{x}[x], x\right]$$