

ΤΥΠΟΛΟΓΙΟ. Γενικές τιμές Green, $\Phi(\vec{x}) = \int_V \rho(\vec{x}') G(\vec{x}, \vec{x}') d\vec{x}' - \frac{1}{4\pi} \int_S \Phi(\vec{x}') \frac{\partial G}{\partial n'} d\alpha' + \frac{1}{4\pi} \int_S G \frac{\partial \Phi}{\partial n'} d\alpha'$
 Green σφαιρικού φλοιού $G(\vec{x}, \vec{x}') = \frac{1}{|\vec{x} - \vec{x}'|} - \frac{a}{x' |\vec{x} - \frac{a^2}{x'^2} \vec{x}'|}$

Πολικές συντεταγμένες, $\vec{\nabla} = \frac{\partial}{\partial r} \vec{e}_r + \frac{1}{r} \frac{\partial}{\partial \theta} \vec{e}_\theta + \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi} \vec{e}_\phi$, $\vec{\nabla}^2 = \frac{1}{r} \frac{\partial}{\partial r} (r^2 \frac{\partial}{\partial r}) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2}{\partial \phi^2} = 0$

$\Phi(r, \theta) = A_0 + B_0 \ln r + \sum (A_n r^n + B_n r^{-n}) (C_n \cos n\theta + D_n \sin n\theta)$
 Σφαιρικές, $\vec{\nabla} = \vec{e}_r \frac{\partial}{\partial r} + \vec{e}_\theta \frac{1}{r} \frac{\partial}{\partial \theta} + \vec{e}_\phi \frac{1}{r \sin \theta} \frac{\partial}{\partial \phi}$, $\Phi(r, \theta, \phi) = \sum_{lm} (A_{lm} r^l + B_{lm} r^{-(l+1)}) Y_{lm}(\theta, \phi)$

Πολυώνυμο Legendre, $P_0(x)=1$, $P_1(x)=x$, $P_2(x)=\frac{1}{2}(3x^2-1)$. $\int_{-1}^1 P_\ell(x) P_{\ell'}(x) dx = \frac{2}{2\ell+1} \delta_{\ell\ell'}$

Σφαιρικές αρμονικές, $Y_{lm}(\theta, \phi) = \sqrt{\frac{2\ell+1}{4\pi} \frac{(\ell-m)!}{(\ell+m)!}} P_\ell^m(\cos \theta) e^{im\phi}$, $P_\ell^m(x) = (-1)^m (1-x^2)^{m/2} \frac{d^m}{dx^m} P_\ell(x)$

Ορθοκανονικότητα Y_{lm} , $\int d\phi \int_0^\pi \sin \theta d\theta Y_{\ell m}^*(\theta, \phi) Y_{\ell' m'}(\theta, \phi) = \delta_{\ell\ell'} \delta_{mm'}$

 $\cos \chi = \cos \theta \cos \theta' + \sin \theta \sin \theta' \cos(\phi - \phi')$

Ορθοκανονικότητα καρτεσιανών,

$$\int_0^{2\pi} \int_0^\pi \sqrt{\frac{2}{\pi}} \sin\left(\frac{n\theta}{2}\right) \sqrt{\frac{2}{\pi}} \sin\left(\frac{m\theta'}{2}\right) d\theta = \delta_{nm}$$

Πολικές, $\int_0^{2\pi} \sin(\theta\phi) \sin(\theta'\phi) d\phi = \pi \delta_{\theta\theta'}$

ΤΥΠΟΛΟΓΙΟ Λαμβάνει in σφαιρικές συντεταγμένες, $\frac{1}{r} \frac{\partial^2}{\partial r^2} (r\psi) + \frac{1}{r^2 \sin \theta} \frac{\partial}{\partial \theta} \left(\sin \theta \frac{\partial \psi}{\partial \theta} \right) + \frac{1}{r^2 \sin^2 \theta} \frac{\partial^2 \psi}{\partial \phi^2} = 0$
 σχέση πλημμελούς $\sum_{lm} Y_{lm}^*(\theta', \phi') Y_{lm}(\theta, \phi) = \delta(r-r') \delta(\cos \theta - \cos \theta') \delta(\phi - \phi')$, $G(\vec{x}, \vec{x}') = \frac{\delta(r-r') \delta(\phi - \phi') \delta(\cos \theta - \cos \theta')}{r^2}$
 Ελλειπτικές διαγρονικές εξισώσεις $\vec{\nabla}^2 \psi(\vec{x}) + [\epsilon(\vec{x}) + \lambda] \psi(\vec{x}) = 0$, $G(\vec{x}, \vec{x}') = 4\pi \sum_n \frac{\psi_n^*(\vec{x}') \psi_n(\vec{x})}{\lambda_n - \lambda}$

Κελυφρικές συντεταγμένες, $\Phi(r, \theta, z) = R(r) Q(\theta) Z(z)$, $R(r) = C J_m(kr) + D N_m(kr)$ ή $Z = E \sinh kr + F \cosh kr$
 ή $R(r) = C I_m(x) + D K_m(x)$ ή $Z(z) = E \sin kz + F \cos kz$
 $\Phi(\phi) = A \cos m\phi + B \sin m\phi$

$$\Phi(\vec{x}) = \frac{q}{r} + \frac{\vec{p} \cdot \vec{x}}{r^3} + \frac{1}{2} \sum_{ij} Q_{ij} \frac{x_i x_j}{r^5} + \dots$$

$$\vec{p} = \int \rho(\vec{x}') \vec{x}' d\vec{x}', \quad Q_{ij} = \int (3x_i x_j - r^2 \delta_{ij}) \rho(\vec{x}') d\vec{x}'$$

$$W = q\Phi(0) - \vec{p} \cdot \vec{E}(0) - \frac{1}{6} \sum_{ij} Q_{ij} \frac{\partial E_j}{\partial x_i}(0) + \dots$$

$$\vec{\nabla} \times \vec{E} = \vec{0}, \quad \vec{\nabla} \cdot \vec{D} = 4\pi \rho, \quad \vec{D} = \vec{E} + 4\pi \vec{P}, \quad \vec{P} = \chi \vec{E}, \quad \vec{D} = \epsilon \vec{E}$$

$$\vec{\nabla} \times \vec{B} = \frac{4\pi}{c} \vec{J}, \quad \vec{\nabla} \cdot \vec{B} = 0, \quad \vec{B} = \mu \vec{H} \quad (\vec{H} = \vec{B} - 4\pi \vec{M}) \quad \vec{H}_{in} = -\frac{4\pi}{c} \vec{M}, \quad \vec{B}_{in} = \frac{8\pi}{c} \vec{M}$$

$$\Phi_M(\vec{x}) = -\vec{\nabla} \cdot \int_V \frac{\vec{M}(\vec{x}')}{|\vec{x} - \vec{x}'|} d\vec{x}', \quad \Phi_N(\vec{x}) = -\int_V \frac{\vec{\nabla}' \cdot \vec{M}(\vec{x}')}{|\vec{x} - \vec{x}'|} d\vec{x}' + \int_S \frac{\hat{n}' \cdot \vec{M}(\vec{x}')}{|\vec{x} - \vec{x}'|} d\alpha'$$

ΤΥΠΟΛΟΓΙΟ $\vec{\nabla} \cdot \vec{D} = 4\pi \rho$, $\vec{\nabla} \cdot \vec{E} = 0$, $\vec{\nabla} \times \vec{E} = -\frac{1}{c} \frac{\partial \vec{B}}{\partial t}$, $\vec{\nabla} \times \vec{H} = \frac{4\pi}{c} \vec{J} + \frac{1}{c} \frac{\partial \vec{E}}{\partial t}$. $\vec{D} = \epsilon \vec{E}$, $\vec{B} = \mu \vec{H}$. $\vec{E} = \vec{\nabla} \times \vec{A}$, $\vec{B} = -\vec{\nabla} \phi - \frac{1}{c} \frac{\partial \vec{A}}{\partial t}$

$$\psi(\vec{x}, t) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} \tilde{\psi}(\vec{x}, \omega) e^{-i\omega t} d\omega, \quad \tilde{\psi}(\vec{x}, \omega) = \int_{-\infty}^{+\infty} \psi(\vec{x}, t) e^{i\omega t} dt$$

$$u_e = \frac{1}{8\pi} \vec{E} \cdot \vec{D}, \quad u_m = \frac{1}{8\pi} \vec{B} \cdot \vec{H}, \quad \vec{S} = \frac{c}{4\pi} (\vec{E} \times \vec{H}), \quad \vec{F} = q(\vec{E} + \frac{\vec{v}}{c} \times \vec{B}), \quad \vec{g} = \frac{1}{4\pi c} (\vec{E} \times \vec{B}) \text{ (σε κενό)}$$

$$\vec{S} = \text{Re} \left[\frac{c}{8\pi} (\vec{E} \times \vec{H}^*) \right], \quad \vec{B} = \frac{c}{\omega} [\vec{k} \times \vec{E}]$$

$$r = r_R + i r_I, \quad \cos r = \cos r_R \cosh r_I - i \sin r_R \sinh r_I, \quad \sin r = \sin r_R \cosh r_I + i \cos r_R \sinh r_I$$

$$\epsilon(\omega) = 1 + \frac{4\pi N e^2}{m} \sum_i f_i (\omega_i^2 - \omega^2 - i\omega \gamma_i)^{-1}, \quad \gamma = \sum f_i \gamma_i, \quad \omega_p^2 = 4\pi N e^2 / m$$

$$\sigma = f_0 N e^2 / [m(\gamma_0 - i\omega)]$$

$$u(x, t) = \frac{1}{\sqrt{2\pi}} \int A(k) e^{ikx - i\omega(k)t} dk, \quad A(k) = \frac{1}{\sqrt{2\pi}} \int u(x, 0) e^{-ikx} dx$$

$$\text{κυκλωμενός} = \text{κυκλωμής} \quad \epsilon(\omega) = 1 + \frac{1}{n_i} P \int_{-\infty}^{+\infty} \frac{[\epsilon(\omega') - 1]}{\omega' - \omega} d\omega'$$