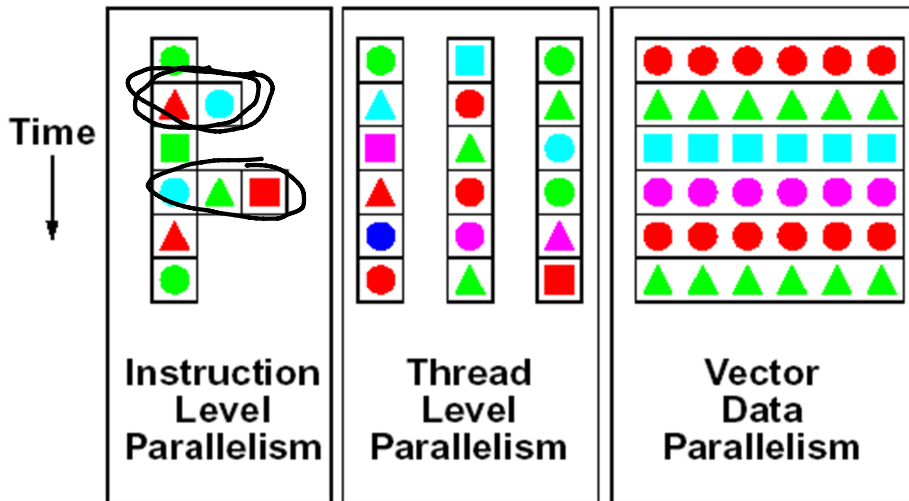
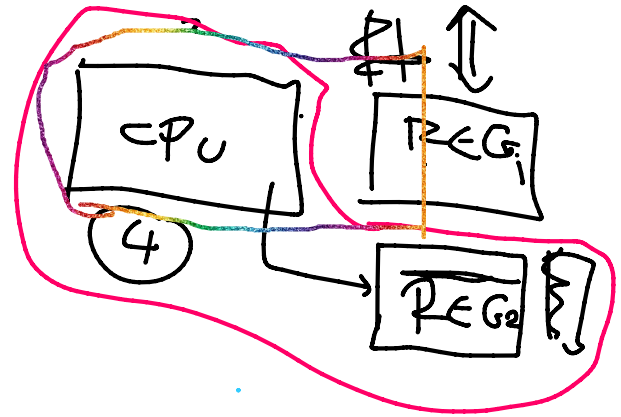


- . Instruction Level Parallelism (ILP)
- . Thread Level Parallelism (TLP)
- . vector Data Parallelism (DP)



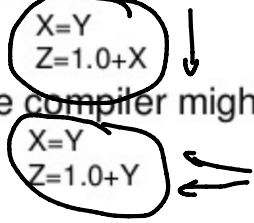
Instruction Level Parallelism (ILP)

- ❖ IPO (Inter-Procedural Optimization)
- ❖ PGO (Profile-Guided Optimization)
- ❖ HLO (High-Level Optimization)

IPO

Copy Propagation

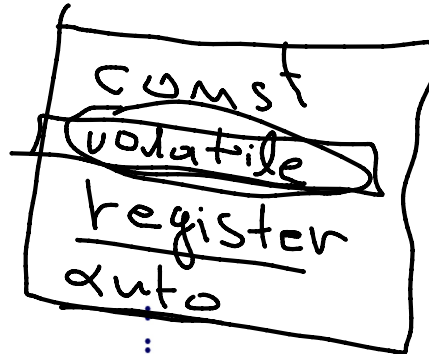
- Consider
 - $X=Y$
 - $Z=1.0+X$
- The compiler might change this to



```

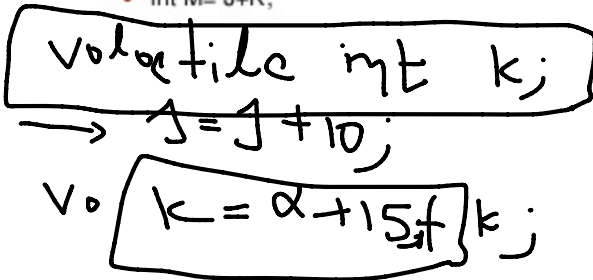
a = 5;
b = 3;
:
:
n = a + b;
for (i = 0; i < n; ++i) {
:
}
    
```

Handwritten annotations: n = 5 + 3; n = 8



Constant Folding

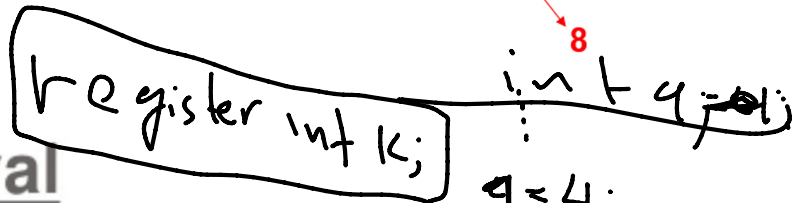
- Consider
 - ~~const~~ int J=100;
 - const int K=200;
 - int M= J+K;



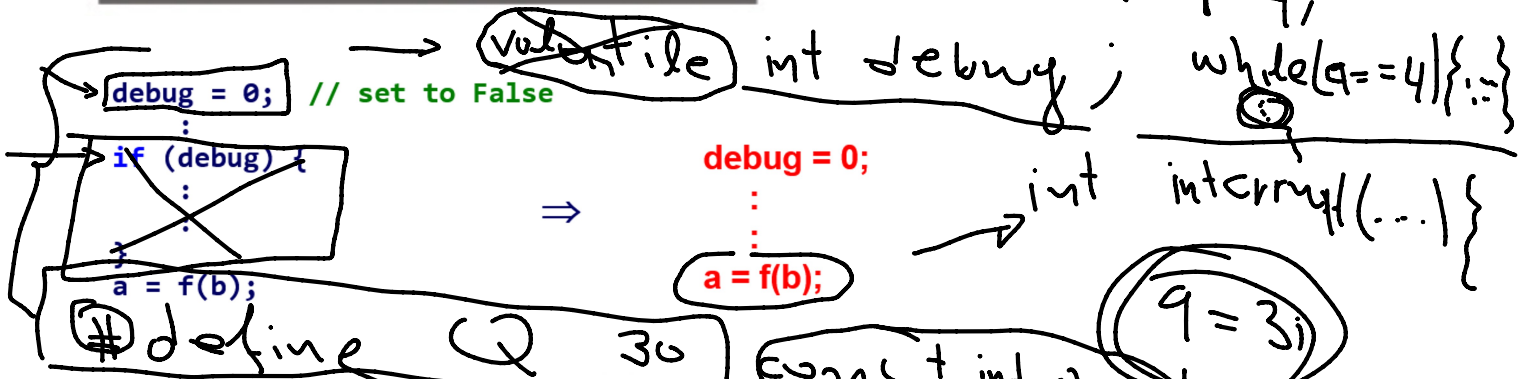
```

n = 5 + 3;
for (i = 0; i < n; ++i) {
:
}
    
```

Handwritten annotations: n = 8



Dead Code Removal



Strength Reduction

- Replace complex or difficult or expensive operations with simpler ones.
 - replacing division by a constant with multiplication by its reciprocal
- Consider
 - $Y=X^{**2}$
 - ✓ Raising a Number to an exponent
 - first X is converted to a logarithm and then multiplied by two and then converted back.
- $Y=X*X$ is much more efficient.
 - Multiplication is Easier than raising a number to a power.

```
int x = 2 * x;
```

```
y <<= 1;
```

```
y = x * x;
```

- $Y=X*X$ is much more efficient.
- Multiplication is Easier than raising a number to a power.

$x = 5$

$(x \ll 2) + x$

$x \ll 2 + x$

$y = x * x;$
 $y = \text{pow}(x, 2.0);$

Induction Variable Simplification


- Consider


```
for(i=1; i<=N; i++)
{
    K=i*4+M;
    C=2*A[K];
    ....
}
```

- Optimized as


```
K=M;
for(i=1; i<=N; i++)
{
    K=K+4;
    C=2*A[K];
    .....
}
```

APX1 ZOMT 15:15

$f(i)$
 $\text{inline int } f(\text{int } i)$ 

Function In-lining & "inline" directive

- Consider


```
for(i=0; i<=N; i++)
{
    ke[i]=kinetic_energy(mass[i], velocity[i]);
}
```

- Optimized as


```
inline float kinetic_energy(float m, float v)
{
    return 0.5*m*v*v;
}
```

```

foo(int z){
  int m = 5;
  return z + m;
}
main(){
  ...
  x = foo(x);
  ...
}

main(){
  ...
  {
    int foo_z = x;
    int m = 5;
    int foo_return = foo_z + m;
    x = foo_return;
  }
  ...
}

main(){
  ...
  x = x + 5;
  ...
}

```

Loop Invariant Conditionals

Consider $N = \dots$

```

DO I=1,K
  IF ( N.EQ.0 ) THEN
    A(I)=A(I)+B(I)*C
  ELSE
    A(I)=0
  ENDIF
ENDDO

```

Optimized as

```

IF ( N.EQ.0 ) then
  DO I=1,k
    A(I)=A(I)+B(I)*C
  ENDDO
ELSE
  DO I=1,K
    A(I)=0
  ENDDO
ENDIF

```

```

for (i=0; i < 100 ; ++i) {
  for (j=0; j < 100 ; ++j) {
    for (k=0 ; k < 100 ; ++k) {
      a[i][j][k] = i*j*k;
    }
  }
}

for (i = 0; i < 100 ; ++i) {
  t1 = a[i];
  for (j = 0 ; j < 100 ; ++j) {
    tmp = i * j;
    t2 = t1[j];
    for (k = 0 ; k < 100 ; ++k) {
      t2[k] = tmp * k;
    }
  }
}

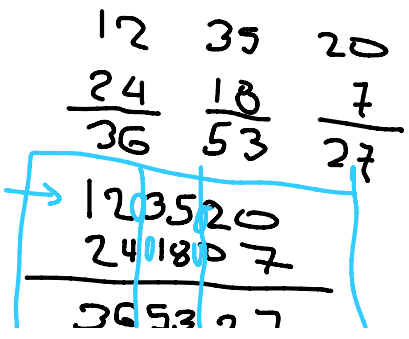
```

req.

Variable Renaming

Consider
 $X = Y * Z$
 $Q = R + X + X$
 $X = A + B$

Optimized as
 $X = Y * Z$
 $q = R + X_ + X_$
 $X = A + B$

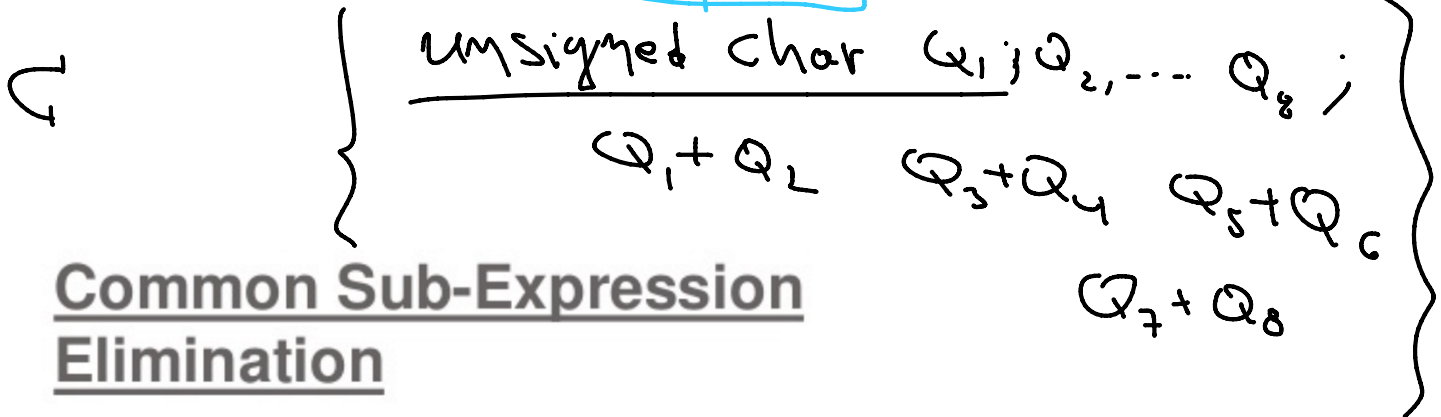


union

$$\boxed{X = A + B}$$

$$\begin{array}{r} 2401807 \\ \hline 365327 \end{array}$$

UNION



Common Sub-Expression Elimination

- Consider

$$\begin{array}{l} A = C * (F + G) \\ D = (F + G) / N \end{array}$$

- Optimized as

$$\begin{array}{l} \text{temp} = F + G \\ A = C * \text{temp} \\ D = \text{temp} / N \end{array}$$

$$\begin{array}{l} a = c * d; \\ \vdots \\ d = (c * d + t) * u \end{array} \Rightarrow \begin{array}{l} a = c * d; \\ \vdots \\ d = (a + t) * u \end{array}$$

Loop Invariant Code Motion

- Consider

```
for(i=0; i<=N; i++)
{
    A[i]=F[i] + C*D;
    E=G[K];
}
```

- Optimized as

```
temp=C*D;
for(i=0; i<=N; i++)
{
    A[i]=F[i] + temp;
}
E=G[K];
```

Loop Fusion

- Consider

```
DO i=1,n  
    x(i) = a(i) + b(i)  
ENDDO  
DO i=1,n  
    y(i) = a(i) * c(i)  
ENDDO
```

- Optimized as

```
DO i=1,n  
    x(i) = a(i) + b(i)  
    y(i) = a(i) * c(i)  
ENDDO
```

Pushing Loops inside Subroutine Calls

Clip slide

- Consider

```
DO i=1,n  
    CALL add(x(i),y(i),z(i))  
ENDDO
```

```
SUBROUTINE add(x,y,z)  
    REAL*8 x,y,z  
    z = x + y  
END
```

- Optimized as

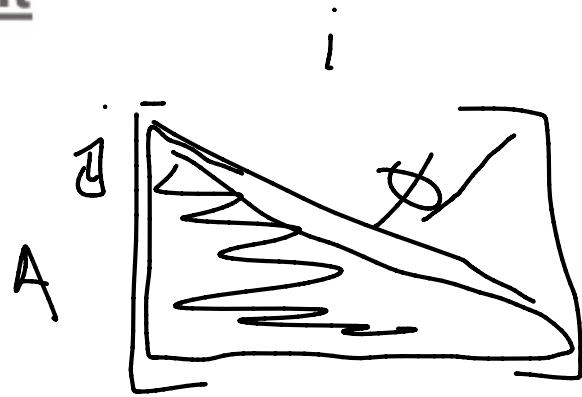
```
CALL add(x(i),y(i),z(i),n)  
  
SUBROUTINE add(x,y,z,n)  
    REAL*8 x(n),y(n),z(n)  
    INTEGER i  
    DO i=1,n  
        z(i)=x(i)+y(i)  
    ENDDO  
END
```

Loop Index Dependent Conditionals

- Consider

```

DO I=1,N
  DO J=1,N
    IF( J.LT.I ) THEN
      A(J,I)=A(J,I) + B(J,I)*C
    ELSE
      A(J,I)=0.0
    ENDIF
  ENDDO
ENDDO
  
```



- Optimized as

```

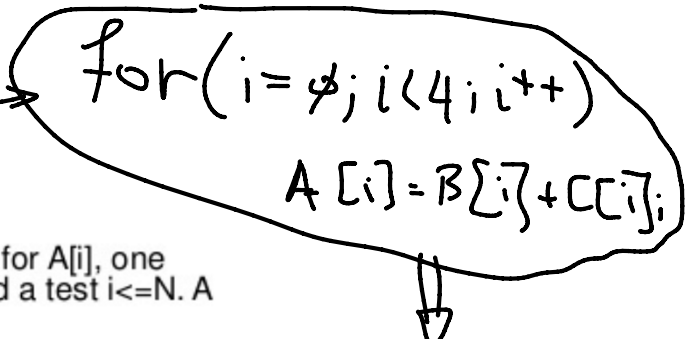
DO I=1,N
  DO J=1,I-1
    A(J,I)=A(J,I) + B(J,I)*C
  ENDDO
  DO J=I,N
    A(J,I)=0.0
  ENDDO
ENDDO
  
```

Loop unrolling

- Consider

```

DO I=1,N
  A[I]=B[I]+C[I]
ENDDO
  
```

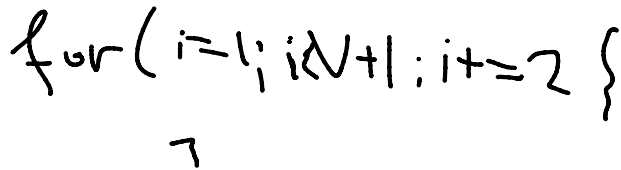


> There are two loads for B[i] and C[i], one store for A[i], one addition B[i]+C[i], another addition for i=i+1 and a test i<=N. A total of six operations.

- Consider

```

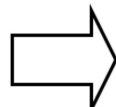
DO I=1,N,2
  A(i)=B(i)+C(i)
  A(i+1)=B(i+1)+C(i+1)
ENDDO
  
```



> four loads, two stores, three additions and one test for a total of ten.

```

j = 0;
while (j < 100){
  a[j] = b[j+1];
  j += 1;
}
  
```



```

j = 0;
while (j < 99){
  a[j] = b[j+1];
  a[j+1] = b[j+2];
  j += 2;
}
  
```



Replace Multiply by Shift

- $A := A * 4;$
 - Can be replaced by 2-bit left shift (signed/unsigned)
 - But must worry about overflow if language does
- $A := A / 4;$

Addition chains for multiplication

- If multiply is very slow (or on a machine with no multiply instruction like the original SPARC), decomposing a constant operand into sum of powers of two can be effective:

$$X * 125 = x * 128 - x * 4 + x$$

- **two shifts, one subtract** and **one add**, which may be faster than one multiply

$$13 * X$$

$X(8 + 4 + 1)$

$$(X \ll 3) + (X \ll 2) + X$$

$4x$

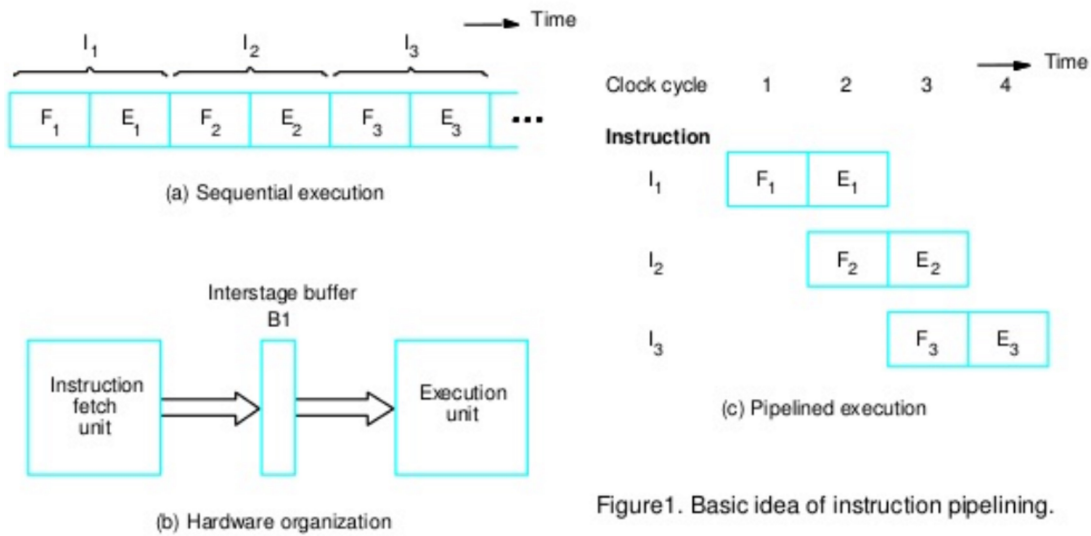
$$13 * X$$

The diagram shows a handwritten derivation of the multiplication of a variable X by the constant 13. It starts with '13 * X' and an upward arrow. Below it, the expression 'X(8 + 4 + 1)' is written. This is followed by '(X << 3) + (X << 2) + X', where the first two terms are grouped together with a horizontal line underneath. To the right, '4x' is circled. At the bottom, a double vertical line separates the expression from the final result '13 * X'.

Instruction Pipelining in CPU

- **Pipelining** improves system performance in terms of throughput.
- Pipelined organization requires sophisticated compilation techniques.

Fetch + Execution



AP×1Z04Me 14:15

Role of Cache Memory

HLO - High Level Optimization

Summary: gcc Optimization Levels

- g:
 - Include debug information, no optimization
- O0:
 - Default, no optimization
- O1:
 - Do optimizations that don't take too long
 - CP, CF, CSE, DCE, LICM, inlining small functions
- O2:
 - Take longer optimizing, more aggressive scheduling
- O3:
 - Make space/speed trade-offs: loop unrolling, more inlining
- Os:
 - Optimize program size

