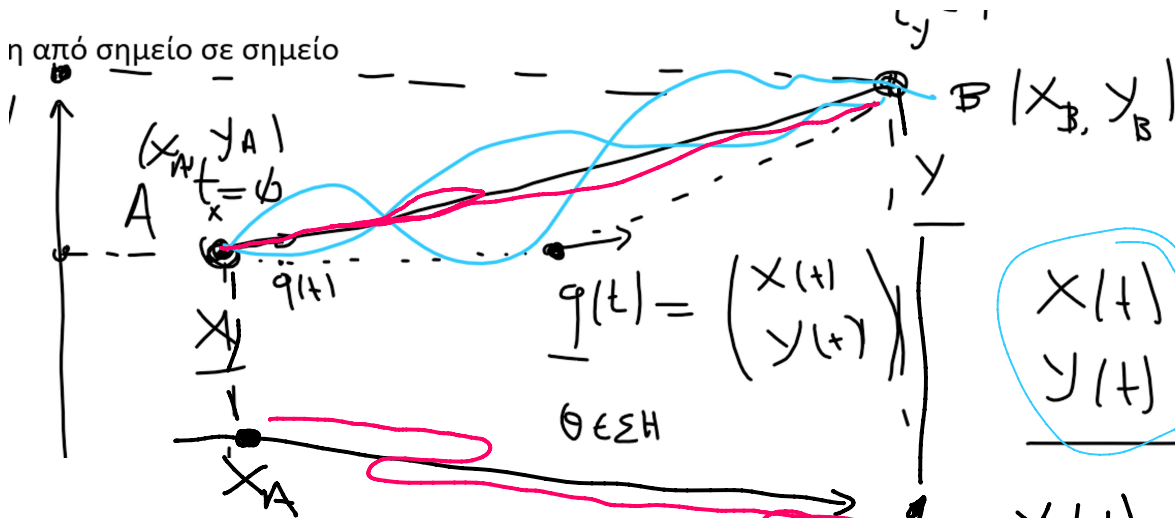


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$$\begin{pmatrix} x(t) \\ y(t) \end{pmatrix}$$

$$\begin{cases} x(\phi) = x_A \\ y(\phi) = y_A \\ x(T) = x_B \\ y(T) = y_B \end{cases}$$

$$x(t) = f(t) \quad x(\phi) = f(\phi) = x_A$$

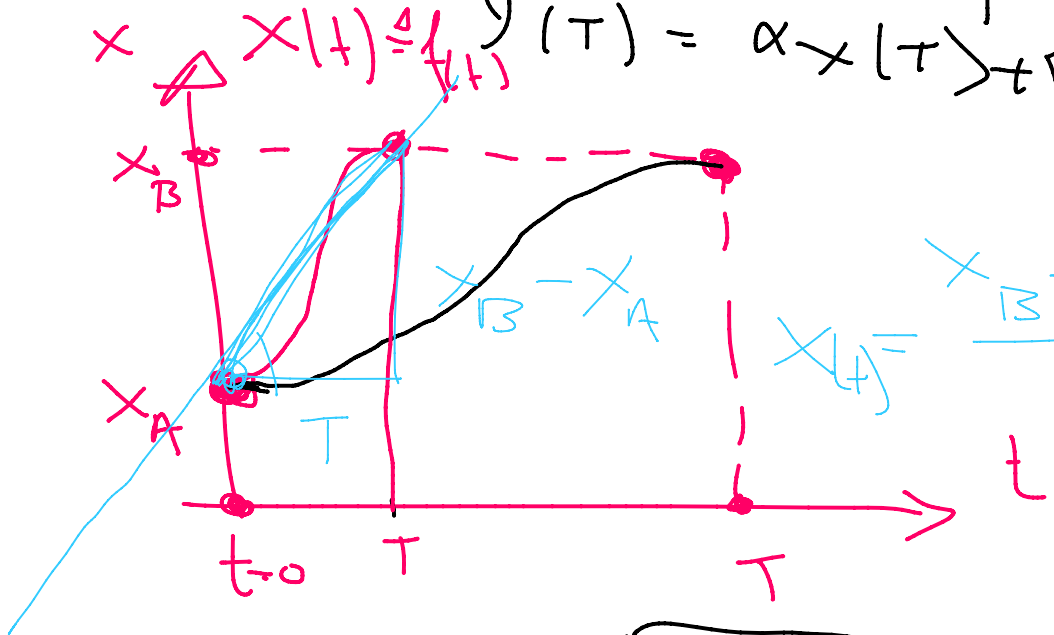
$$x(T) = f(T) = x_B$$

$$y(t) = \alpha x(t) + \beta$$

$$y(\phi) = \alpha x(\phi) + \beta = \alpha x_A + \beta = y_A$$

$$y(T) = \alpha x(T) + \beta = \alpha x_B + \beta = y_B$$

$$\begin{cases} \alpha = \dots \\ \beta = \dots \end{cases}$$



$$\frac{\Delta x}{\Delta t} = v$$

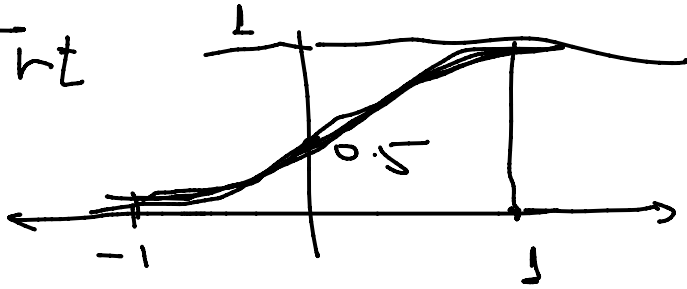
$$\begin{cases} \dot{x}(\phi) = \dot{\phi} \\ \dot{y}(\phi) = \dot{\phi} \\ \dot{x}(T) = \dot{\phi} \\ \dot{y}(T) = \dot{\phi} \end{cases}$$

Δt

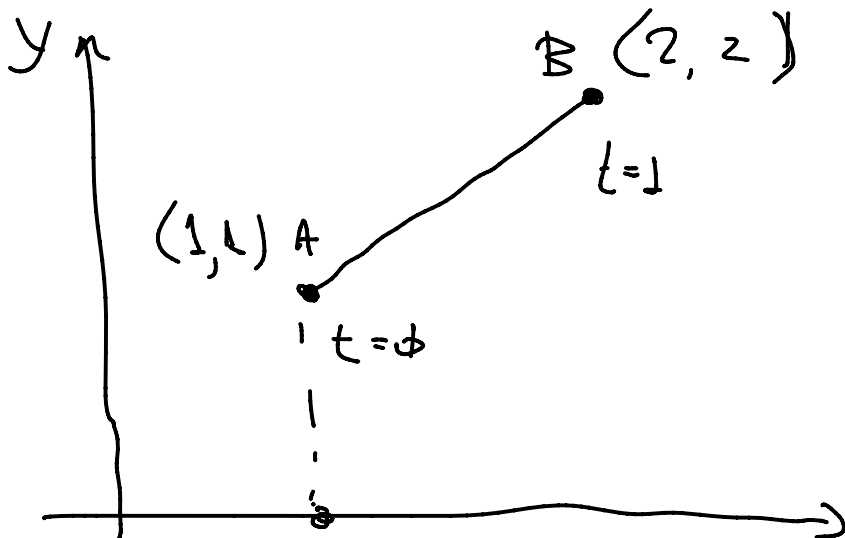
$$\left\{ \begin{array}{l} X(\tau) = \phi \quad Y(\tau) = \phi \\ X(\phi) = X_A \\ X(\tau) = X_B \end{array} \right.$$

$$X(t)$$

$$f(t) = \frac{1}{1 + e^{-rt}}$$



$$g(t) = \left\{ \begin{array}{l} X(t) = \frac{\beta - X_A}{\tau} \cdot t + X_A \\ Y(t) = \alpha X(t) + \beta \end{array} \right.$$



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12:20

$$\left\{ \begin{array}{l} X_A = 1 \\ X_B = 2 \end{array} \right.$$

$$\left\{ \begin{array}{l} Y_A = 1 \\ Y_B = 2 \end{array} \right.$$

$$Y_B = 2$$

x

$$\begin{cases} \alpha x_A + \beta = y_A \\ \alpha x_B + \beta = y_B \end{cases}$$

\Rightarrow

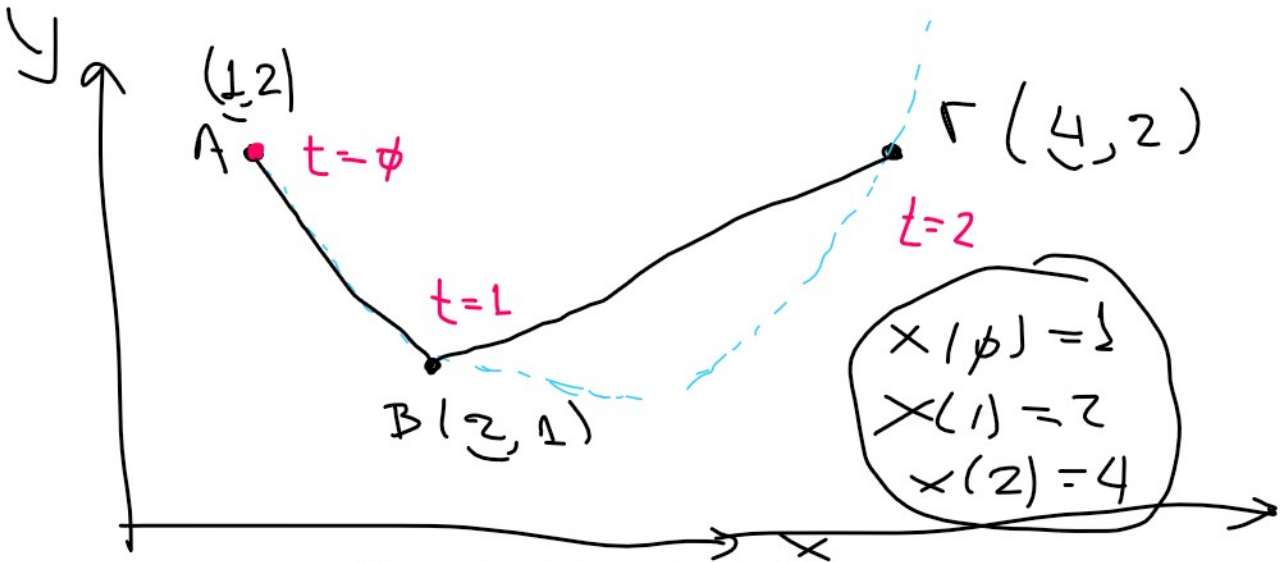
$$\begin{cases} \alpha + \beta = 1 \\ 2\alpha + \beta = 2 \end{cases}$$

$$\alpha = 1 \Rightarrow \beta = 0$$

$$\alpha = 1$$

$$y(t) = x(t)$$

$$q(t) = \begin{cases} x(t) = t + 1 \\ y(t) = t + 1 \end{cases}$$



$$x(t) = S_1 t^3 + S_2 t^2 + S_3 t + S_4 = 1$$

$$y(t) =$$

$$S_4 = x(0) = 1$$

$$x(0) = x_A = 1$$

$$x(1) = x_B = 2$$

$$x(2) = x_\Gamma = 4$$

$$y(t) = \alpha x^2(t) + \beta x(t) + \gamma$$

$$y(t) = \alpha x(t) + \beta x'(t) + \gamma$$

$$\begin{cases} 2 = \alpha + \beta + \gamma \\ 1 = 4\alpha + 2\beta + \gamma \end{cases} \Rightarrow 3\alpha + \beta = -1$$

$$2 = 16\alpha + 4\beta + \gamma$$

$$x(t) = S_1 t^3 + S_2 t^2 + S_3 t + S_4$$

$$x(t) = S_2 t^2 + S_3 t + S_4$$

$$x(0) = 1 \Rightarrow S_4 = 1$$

$$x(1) = 2 = S_2 + S_3 + 1 \Rightarrow S_2 + S_3 = 1$$

$$x(2) = 4 = 4S_2 + 2S_3 + 1 = 4 \Rightarrow$$

$$S_2 + S_3 = 1$$

$$4S_2 + 2S_3 = 3$$

$$2s_2 + 2s_3 = 2$$

$$2s_2 = 1 \Rightarrow s_2 = \frac{1}{2}$$

$$s_3 = \frac{1}{2}$$

$$x(t) = \frac{1}{2}t^2 + \frac{1}{2}t + 1$$

$$y(t) = \alpha x(t) + \beta \dot{x}(t) + \gamma$$

$$\underline{v}(\phi) = \underline{\dot{\varphi}}(\phi) = \left\{ \begin{array}{l} \dot{x}(\phi) \\ \dot{y}(\phi) \end{array} \right\} =$$

$$= \left\{ \begin{array}{l} t + \frac{1}{2} \Big|_{t=\phi} \\ 2\alpha x(t) \dot{x}(t) + \beta \dot{x}(t) \Big|_{t=\phi} \end{array} \right.$$

$$\dot{x}(\phi) = \phi$$

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$$x(\phi) = \phi$$

$$\dot{x}(\phi) = \phi$$

$$x(t) = S_1 t^3 + S_2 t^2 + S_3 t + S_4$$

$$x(\phi) = 1 \Rightarrow \boxed{S_4 = 1}$$

$$x(1) = 2 \Rightarrow S_1 + S_2 + \cancel{S_3} + 1 = 2$$

$$x(2) = 4 \Rightarrow \cancel{8S_1} + 4S_2 + \cancel{2S_3} + 1 = 4$$

$$\dot{x}(\phi) = \phi \Rightarrow \boxed{S_3 = \phi}$$

$$S_1 + S_2 = 1 \Rightarrow$$

$$\cancel{8}S_1 + 4S_2 = 3$$

$$4S_1 + 4S_2 = 4$$

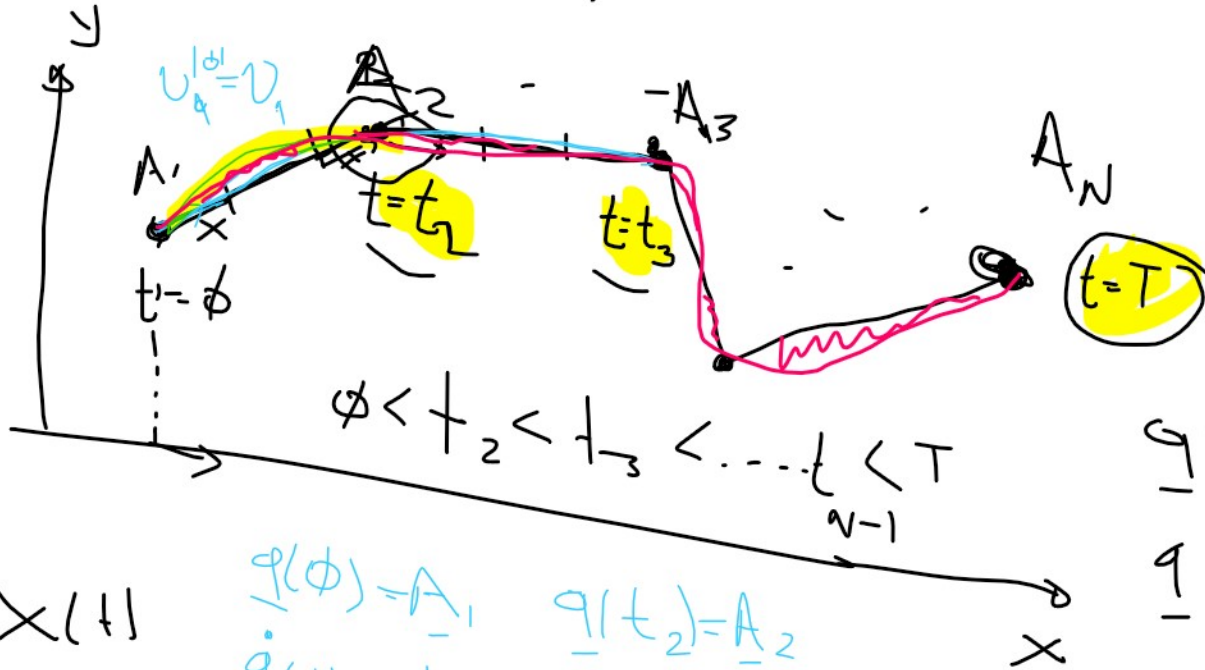
$$\boxed{S_2 = \frac{5}{4}}$$

$$4S_1 = -1 \Rightarrow \boxed{S_1 = -\frac{1}{4}}$$

$$x(t) = -\frac{1}{4}t^3 + \frac{5}{4}t^2 + 1 \quad \text{q/w}$$

$$\left. \begin{aligned} y(t) = \alpha x^2(t) + \beta x(t) + \gamma \end{aligned} \right\} = \underline{q(t)}$$

$$y(\phi) = ? = \phi$$



$$\phi < t_2 < t_3 < \dots < t < T$$

$$\underline{q}(t_2) = \underline{A}_2$$

$$\underline{q}(t_3) = \underline{A}_3$$

$$\dots$$

$$\underline{q}(t_{n-1}) = \underline{A}_{n-1}$$

$$\underline{q}(T) = \underline{A}_N$$

$$x(t)$$

$$y(t)$$

$$\dot{x}(\phi) = \dot{x}_{A_1}$$

$$\dot{y}(\phi) = \dot{y}_{A_1}$$

$$\underline{q}(\phi) = \underline{A}_1$$

$$\dot{\underline{q}}(\phi) = \underline{v}_{A_1}$$

$$\underline{q}(t_2) = \underline{A}_2$$

$$\dot{\underline{q}}(t_2^+) = \dot{\underline{q}}(t_2^-)$$

$$\ddot{\underline{q}}(t_2^+) = \ddot{\underline{q}}(t_2^-)$$

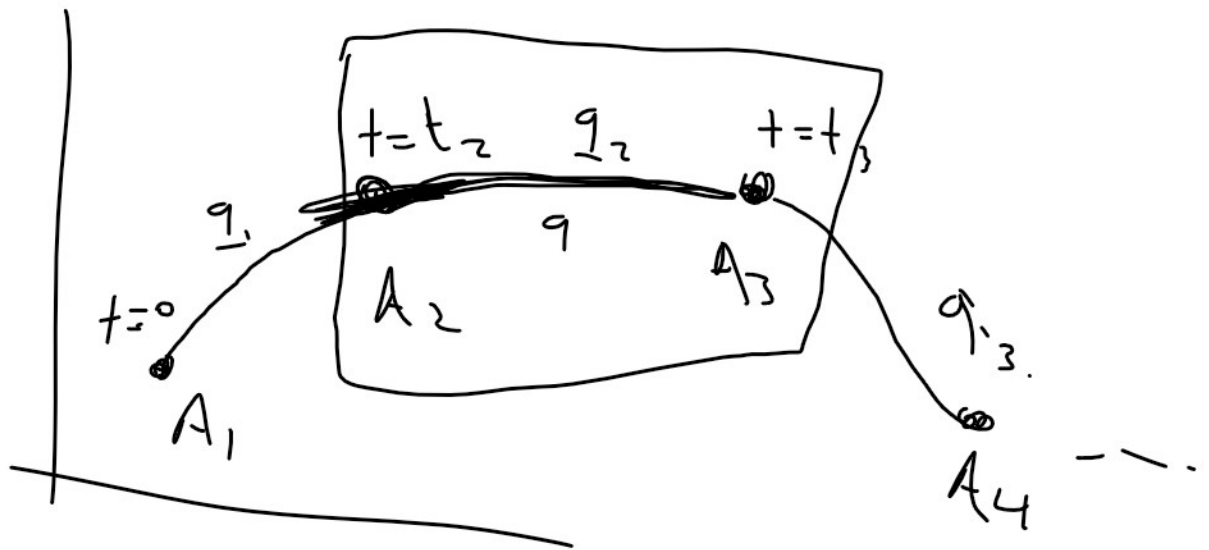
$$x(\phi) = x_{A_1}$$

$$y(\phi) = y_{A_1}$$

$$\underline{q}(\phi) = \underline{A}_1$$

$$\dot{\underline{q}}(\phi) = \underline{v}_{A_1}$$

$$\underline{q}(T) = \underline{A}_N$$



$$q(t) = \begin{cases} \dots & t_2 < t < t_3 \\ \dots & \dots \end{cases}$$

$$q(t=t_{2-}) = q(t=t_{2+}) = A_2$$

$$\dot{q}_1(t=t_{2-}) = \dot{q}_2(t=t_{2+})$$

$$\ddot{q}_1(t=t_2) = \ddot{q}_2(t=t_{2+})$$

$$\left. \frac{\partial y_{q_1}}{\partial x_{q_1}} \right|_{t=t_{2-}} = \left. \frac{\partial y_{q_2}}{\partial x_{q_2}} \right|_{t=t_{2+}}$$

$$|\dot{q}(t)| < |V_{max}|$$

$$|(\dot{x})| < |v_{max}|$$

